

## Evaporative cooling of a small number of atoms in a single-beam microscopic dipole trap

R Bourgain, J Pellegrino, A Fuhrmanek, Yvan R. P. Sortais, Antoine Browaeys

► **To cite this version:**

R Bourgain, J Pellegrino, A Fuhrmanek, Yvan R. P. Sortais, Antoine Browaeys. Evaporative cooling of a small number of atoms in a single-beam microscopic dipole trap. *Physical Review A*, American Physical Society, 2013, 88, pp.23428 / arXiv:1305.3802. 10.1103/PhysRevA.88.023428 . hal-01102107

HAL Id: hal-01102107

<https://hal-iogs.archives-ouvertes.fr/hal-01102107>

Submitted on 12 Jan 2015

**HAL** is a multi-disciplinary open access archive for the deposit and dissemination of scientific research documents, whether they are published or not. The documents may come from teaching and research institutions in France or abroad, or from public or private research centers.

L'archive ouverte pluridisciplinaire **HAL**, est destinée au dépôt et à la diffusion de documents scientifiques de niveau recherche, publiés ou non, émanant des établissements d'enseignement et de recherche français ou étrangers, des laboratoires publics ou privés.

**Evaporative cooling of a small number of atoms in a single-beam microscopic dipole trap**

R. Bourgain, J. Pellegrino, A. Fuhrmanek, Y. R. P. Sortais,\* and A. Browaeys

*Laboratoire Charles Fabry, Institut d'Optique, CNRS, Université Paris Sud, 2 Avenue Augustin Fresnel, 91127 Palaiseau Cedex, France*

(Received 16 May 2013; published 30 August 2013)

We demonstrate experimentally the evaporative cooling of a few hundred rubidium-87 atoms in a single-beam microscopic dipole trap. Starting with 800 atoms at a temperature of  $125\ \mu\text{K}$ , we produce an unpolarized sample of 40 atoms at  $110\ \text{nK}$ , within 3 s. The phase-space density at the end of the evaporation reaches unity, close to quantum degeneracy. The gain in phase-space density after evaporation is  $10^3$ . We find that the scaling laws used for much larger numbers of atoms are still valid despite the small number of atoms involved in the evaporative cooling process. We also compare our results to a simple kinetic model describing the evaporation process and find good agreement with the data.

DOI: [10.1103/PhysRevA.88.023428](https://doi.org/10.1103/PhysRevA.88.023428)

PACS number(s): 37.10.De, 37.10.Gh, 64.70.fm, 67.85.Hj

**I. INTRODUCTION**

Mesoscopic atomic ensembles containing a few hundred ultracold atoms constitute an interesting system for fundamental studies as well as applications in quantum optics and atomic physics. For example, they have been proposed as a tool to observe nonlinear effects at the single-photon level, e.g., using Rydberg atomic states [1], and more generally for applications in quantum information [2,3]. Recent proof-of-principle experiments along this line have been performed using samples containing  $\sim 100$  laser-cooled atoms held in a microscopic dipole trap [4] or in one-dimensional optical lattices [5]. As another example, a quasideterministic single-atom source has recently been demonstrated using light-assisted collisions in a small cold atomic ensemble [6]. These demonstrations have been achieved with atomic samples laser-cooled around the Doppler temperature, but it is often desirable to start from much colder atoms to decrease the sources of decoherence during quantum manipulations. Moreover, when further cooled down, these systems could allow the study of quantum degenerate gases in a regime where the number of atoms is small. An important experiment in this direction has been performed recently with fermions held in a tight dipole trap [7].

Several strategies can be used to prepare small ultracold atomic ensembles with temperatures in the micro-Kelvin range. One of them relies on the production of a macroscopic quantum degenerate or nearly degenerate gas as a preliminary step; the ultracold sample is then used as a source to load a dipole trap in a dimple configuration, as demonstrated in Refs. [8] and [9] for large atomic samples and in Ref. [7] for a few tens of fermionic atoms. An alternate route bypasses the first step mentioned above and starts directly with a small sample of laser-cooled atoms confined in a tight trap of typically several-micrometer size, such as magnetic traps on an atom chip [10] or arrays of optical dipole traps [11]. Evaporative cooling then allows reduction of the temperature (see, e.g., [12] and [13] and references therein) and has led so far to condensed samples containing several thousand atoms.

In the present work, we follow the second route and extend evaporative cooling to low atom numbers, ranging from a few hundreds to a few tens. Here, we use unpolarized

rubidium atoms held in a single-beam microscopic dipole trap. Despite its simplicity, we show that this configuration is compatible with high elastic collision rates and leads to efficient evaporation. To do so, we lower the trap depth, as originally demonstrated by Adams *et al.* [14] and now routinely implemented in many laboratories to achieve quantum degenerate gases (see, e.g., [15–22]), by merely decreasing the power of the trap laser. We observe that the phase-space density increases by 3 orders of magnitude during the evaporation and eventually reaches unity, with clouds containing as few as 40 atoms at  $110\ \text{nK}$ . We also find that despite the small number of atoms involved, the scaling laws that govern the evolution of the thermodynamical quantities, derived by O'Hara *et al.* [23], are still valid. Finally, we show that a simple kinetic model of the evaporative cooling process inspired by the works of Refs. [12,23] and [24] reproduces our data well.

The paper is organized as follows. In Sec. II, we describe our setup and the experimental procedures. In particular, we detail our strategy to load the microscopic dipole trap efficiently with up to 800 atoms at a temperature around  $125\ \mu\text{K}$ . Section III presents our results on evaporative cooling and compares the evolution of the temperature and the phase-space density to the scaling laws. In Sec. IV, we compare our data to the model in Refs. [12,23] and [24]. We conclude with possible improvements of evaporative cooling in single-beam-based experiments in Sec. V.

**II. EXPERIMENTAL SETUP AND PROCEDURES**

Our setup is illustrated in Fig. 1. We trap laser-cooled rubidium-87 atoms in a microscopic dipole trap produced by focusing a laser beam at  $957\ \text{nm}$  with a large-numerical-aperture aspheric lens, as described in Ref. [25]. The  $1/e^2$  radius of the Gaussian spot is  $w = 1.6\ \mu\text{m}$ . The size of the trap along the longitudinal direction is characterized by the Rayleigh length,  $z_R = 8.4\ \mu\text{m}$ . We use 20 mW of laser power to achieve a trap depth  $U/k_B = 1\ \text{mK}$  ( $k_B$  is the Boltzman constant). For this depth, the trapping frequencies of the atoms in the transverse and longitudinal directions are  $\omega_{\perp}/2\pi = 64\ \text{kHz}$  and  $\omega_{\parallel}/2\pi = 9\ \text{kHz}$ , respectively. For a temperature of  $125\ \mu\text{K}$ , this corresponds to a thermal cloud with root-mean-square sizes of  $270\ \text{nm}$  and  $2\ \mu\text{m}$ , respectively.

For all the measurements reported here, we measure the number of atoms  $N$  after the cloud has been released in

\*yvan.sortais@institutoptique.fr

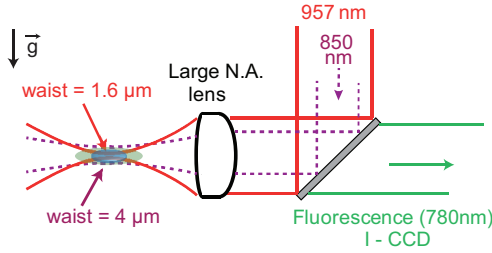


FIG. 1. (Color online) Trapping and detection scheme showing the two super-imposed single-beam dipole traps (see text) with comparable depths ( $\sim 1$  mK) but different sizes (waists  $4 \mu\text{m}$  and  $1.6 \mu\text{m}$ ). The large-numerical-aperture lens collects light-induced fluorescence. Imaging with an intensified camera (I-CCD) enables atom counting and temperature measurements, from which we extract the phase-space density.  $\vec{g}$  indicates the direction of gravity.

free space. For that purpose, we send a  $10\text{-}\mu\text{s}$  pulse of circularly polarized probe light resonant with the  $|5S_{1/2}, F=2, M=2\rangle$ -to- $|5P_{3/2}, F'=3, M'=3\rangle$  transition, combined with repumping light tuned to the  $(5S_{1/2}, F=1)$ -to- $(5P_{3/2}, F=2)$  transition. The intensity of the probe beam is  $I/I_{\text{sat}} = 1$  ( $I_{\text{sat}} = 1.6 \text{ mW/cm}^2$ ). The large-numerical-aperture aspheric lens collects the light-induced fluorescence, which we detect with an image intensifier followed by a low-noise charge-coupled-device camera (I-CCD). The duration of the time of flight is chosen long enough for the density to drop below  $10^{11}$  at/cm<sup>3</sup> to avoid light-assisted losses during probing [26]. In this way, the detected fluorescence is proportional to the number of atoms, which we extract by calibrating our detection system with a single atom [27]. The small number of atoms  $N$  requires that we integrate the signal over several realizations of the experiment, typically 10 to 1000 for  $N$  ranging from 800 to 40, allowing us to determine  $N$  with a typical statistical uncertainty of 10%. We measure the temperature  $T$  of the cloud with the time-of-flight technique with a statistical uncertainty of 10%.

Efficient evaporative cooling requires a high elastic collision rate and therefore that we initially confine a large number of atoms in the microscopic dipole trap. To do so, we proceed in four steps: first, we load a magneto-optical trap (MOT) in 1 s using a Zeeman slower. In the second step, we load from this MOT a dipole trap with a  $1/e^2$  radius of  $4 \mu\text{m}$  and a depth of  $1.4 \text{ mK}$  (see Fig. 1) produced by focusing a laser beam at  $850 \text{ nm}$  with the above-mentioned aspheric lens (the full aperture of the lens is not used here). For this purpose, we use a compressed MOT sequence during which we reduce the intensity of the MOT lasers while red-detuning them from the fluorescence resonance. This results in a cloud of up to 3500 atoms at a temperature of  $200 \mu\text{K}$  and in a mixture of Zeeman sublevels  $M = 0, \pm 1$  of the  $F = 1$  hyperfine ground state. In the third step, we switch off the MOT lasers and turn on the microscopic dipole trap ( $w = 1.6 \mu\text{m}$ , depth of  $1 \text{ mK}$ ), which acts as a dimple. Finally, after 200 ms, we switch off the  $4\text{-}\mu\text{m}$  trap, and following 60 ms of plain evaporation,  $\sim 20\%$  of the atoms initially in the  $4\text{-}\mu\text{m}$  trap are left in the microscopic dipole trap.

At the end of the loading procedure,  $N \approx 800$  atoms are trapped in the  $U/k_B = 1 \text{ mK}$  deep microscopic trap, at a temperature  $T \approx 125 \mu\text{K}$ . The atoms are prepared in the  $F = 1$  hyperfine ground-state level, in a mixture of Zeeman substates. Assuming a deep harmonic trap, the thermal volume

is  $V_{\text{th}} = [2\pi k_B T / (m\omega^2)]^{3/2}$ , corresponding to a spatial density at the center of the trap  $n_0 = N/V_{\text{th}} \approx 3 \times 10^{14}$  at/cm<sup>3</sup> and an initial phase-space density  $D = N(\hbar\omega/k_B T)^3 \approx 1.5 \times 10^{-3}$ . Here,  $\omega = (\omega_1^2 \omega_{\parallel})^{1/3}$  is the mean oscillation frequency of the trap. Note that the phase-space density calculated in this way is based on the total number of atoms, irrespective of their Zeeman sublevel. In the present status of the experiment we do not measure the population in each Zeeman state. We calculate the elastic collision rate  $\gamma_{\text{el}} = n_0 \sigma \bar{v} \sqrt{2} \approx 3 \times 10^4 \text{ s}^{-1}$ . Here,  $\bar{v} = \sqrt{8k_B T / (\pi m)}$  is the thermal average velocity ( $m$  is the atomic mass). The effective elastic cross section is  $\sigma = \epsilon 4\pi a^2$  with  $\epsilon = 2$  or  $4/3$  for, respectively, atoms all in the same Zeeman sublevel of  $F = 1$  or atoms in an equal mixture of Zeeman substates. Here,  $a = 5 \text{ nm}$  is the scattering length.

### III. EXPERIMENTAL RESULTS AND COMPARISON TO SCALING LAWS

Once the microscopic dipole trap has been loaded, we apply forced evaporation by decreasing the power of the dipole trap beam using an acousto-optical modulator. We calculate the depth  $U(t)$ , assuming a Gaussian laser beam and taking into account the deformation of the dipole potential by gravity. The evaporation ramp consists of 10 pieces, each piece corresponding to a linear decrease in the trap depth. At the end of each step, we maximize the phase-space density by adjusting the duration of the linear piece [28]. The experimental ramp obtained in this way is represented in Fig. 2.

For the sake of comparison we also plot the theoretical ramp predicted by O'Hara *et al.* [23], which is valid when the ratio  $\eta = U/(k_B T)$  remains constant throughout the evaporation. Also, this prediction holds in the absence of inelastic losses.

In that case, the ramp is  $U(t) = U_i(1 + t/\tau)^{\frac{2(3-\eta')}{\eta'}}$ , with  $U_i$  the initial trap depth,  $\eta' = \eta + \kappa$ , and  $\kappa = (\eta - 5)/(\eta - 4)$  when  $\eta \gg 1$ . The time constant  $\tau$  is related to  $\eta$  and the initial elastic collision rate  $\gamma_{\text{el},i}$  through  $\tau = (\frac{2}{3}\eta'(\eta - 4)e^{-\eta}\gamma_{\text{el},i}/(2\sqrt{2}))^{-1}$ , of the order of 15 ms, using our initial measured value,  $\eta \approx 8.5$ .

Not surprisingly, the experimental ramp deviates from the above-mentioned theoretical prediction, especially in the early stage of evaporation. This is due to the underlying assumptions of the prediction not being fulfilled in our case. Figure 3(a) shows that  $\eta$  decreases rapidly at the beginning of

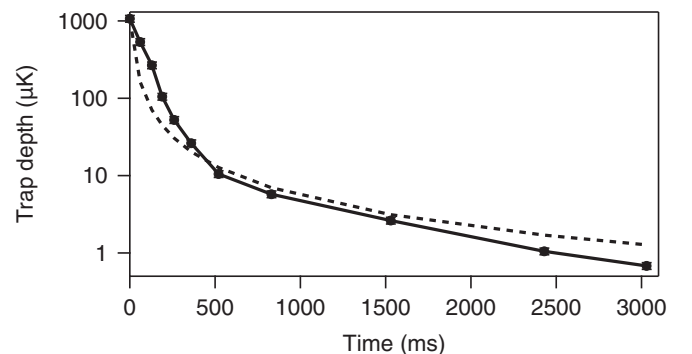


FIG. 2. Evolution of the trap depth as a function of time during evaporation. Solid line: experimental ramp with linear pieces after optimization. The trap depth is measured with a 10% uncertainty. Dotted line: theoretical prediction by O'Hara *et al.* [23].

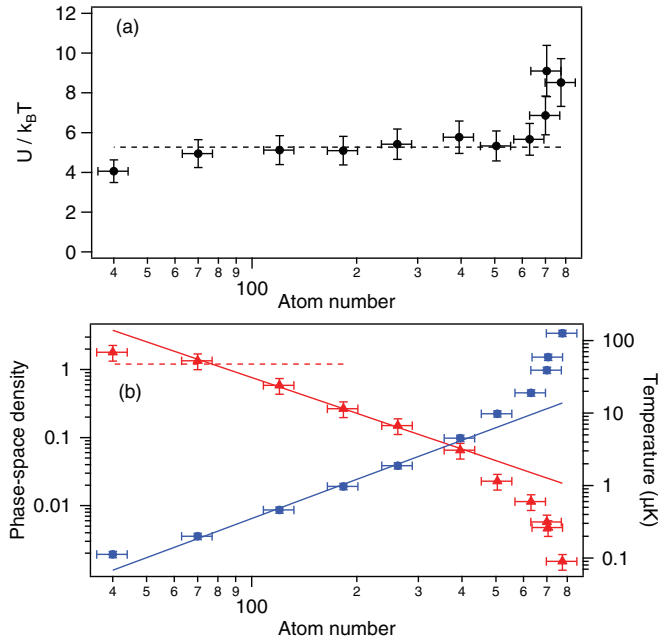


FIG. 3. (Color online) (a) Evolution of the ratio  $\eta = U/k_B T$  versus the number of atoms  $N$  during evaporation (filled circles). Dashed line: average value of  $\eta$  for  $70 \leq N \leq 400$ . (b) Evolution of the measured temperature  $T$  (filled circles; right axis) and the phase-space density  $D = N(\hbar\omega/k_B T)^3$  (triangles; left axis) versus the number of atoms. Solid lines are fits by power laws performed for data corresponding to  $70 \leq N \leq 400$ . Error bars correspond to 10% uncertainties on the measured temperature, number of atoms, trap depth  $U$ , and oscillation frequency  $\omega$ . In (b), the horizontal dashed line at value  $D = \zeta(3) \simeq 1.202$  indicates the transition between a thermal and a degenerate polarized sample.

the evaporation, before it stabilizes around 5. It is therefore not constant throughout evaporation and not much larger than 1. Moreover, in our case, the inelastic losses are not negligible at the beginning of the evaporation ramp (see Sec. IV). We also note that the initial elastic collision rate is of the order of the oscillation frequency  $\omega_{||}$  along the longitudinal axis of the trap. The cloud may therefore be partially in the hydrodynamics regime (see, e.g., [29]), an effect not taken into account here.

Figure 3(b) shows the evolution of the temperature versus the atom number during the evaporation. Combining the temperature and the number of atoms measured at the end of each linear piece of the ramp with the knowledge of the trap depth  $U$ , we calculate the average oscillation frequency  $\omega$  and the phase-space density  $D = N(\hbar\omega/k_B T)^3$  at the center of the trap, assuming an infinitely deep harmonic trap. The evolution of  $D$  is also represented in Fig. 3(b): we observe a gain in phase-space density of  $10^3$  during evaporation. The data suggest that, assuming a polarized sample, we may have reached quantum degeneracy at the end of the ramp, as  $D$  then exceeds the threshold value  $\zeta(3) \simeq 1.202$  [with the usual definition of the Riemann function  $\zeta(n) = \sum_{j=1}^{\infty} 1/j^n$ ] [30]. However, we could not see any evidence of a double-structure on the column density after time of flight. This fact may be due to the small number of atoms involved [30]: at the threshold,  $k_B T_c \approx \hbar\omega(N/\zeta(3))^{1/3} \approx 3\hbar\omega$ . This implies that the thermal and the quantum degenerate components of the gas would have

very similar sizes in a time-of-flight measurement (the ratio of the two sizes is  $\sim \sqrt{k_B T/(\hbar\omega)}$  in the absence of interaction between atoms). Furthermore, we do not have any access to the anisotropy of the cloud due to the geometry of the experiment, as we look along the long axis of the traps (see Fig. 1). More involved diagnostics will be necessary to study the quantum degenerate regime, such as stimulated Raman spectroscopy [31–33], which we leave for future work.

As a first step to understand evaporation processes in our single-beam trapping configuration, we compare the data in Fig. 3(b) to the scaling laws derived by O'Hara *et al.* [23], which are valid for a constant ratio  $\eta$  and in the absence of inelastic losses. Following [23], the phase-space density should scale as  $D \propto N^{-\xi}$ , with  $\xi = \eta' - 4$  characterizing the efficiency of evaporation [13]. In the same way, the temperature is expected to scale with the number of atoms as  $T \propto N^{2(\eta'-3)/3}$ . We have fitted the scaling laws to the data for which  $\eta$  is almost constant, i.e.,  $70 \leq N \leq 400$  [see Fig. 3(a)]. We find that  $d \ln T / d \ln N = 1.79(6)$  and that the efficiency of evaporation is  $\xi = 1.75(5)$ . These two values lead to two independent and consistent evaluations of  $\eta = 5.4(1)$  [34]. In the above-mentioned range for  $N$ , the scaling laws are also consistent with the average ratio  $\eta = 5.3(3)$ , which we directly deduce from  $U$  and  $T$  [see Fig. 3(a)]. Thus, inasmuch as the ratio  $\eta$  remains constant and the inelastic losses can be neglected (which is the case for  $N \leq 400$ ; see Sec. IV), the scaling laws predicted by O'Hara *et al.* are valid even for the small value  $\eta \sim 5$  and atom numbers as small as a few tens.

#### IV. EVAPORATION DYNAMICS

In order to better understand the evaporation processes involved in our geometry, in particular, the effect of the inelastic losses at the beginning of the evaporation process ( $N > 400$ ), we have simulated the evaporative cooling process using the kinetic model developed in Refs. [12,23] and [24]. This model assumes that the atomic cloud is in thermal quasiequilibrium at any time during evaporation, that it is described by a truncated Boltzmann distribution, and that the atomic trajectories are ergodic. Based on these assumptions, one calculates thermodynamical quantities for the gas and relates them through rate equations. Here, we include in the model one-, two-, and three-body inelastic losses, as well as heating due to spontaneous emission induced by the trapping laser, and we take into account the time dependence of the parameter  $\eta$ .

We start with the average energy of the atomic cloud assumed to be trapped in a deep harmonic potential,  $E = 3Nk_B T$ , which yields  $\dot{E}/E = \dot{N}/N + \dot{T}/T$ . Four mechanisms lead to a variation in the energy during evaporation. The first one is evaporation due to elastic collisions between trapped atoms. Atoms leaving the trap have an average energy  $(\eta + \kappa)k_B T$ , with  $\kappa = (\eta - 5)/(\eta - 4)$  [35]. Assuming three-dimensional evaporation, this mechanism leads to a rate of variation in the energy  $\dot{E}_{ev} = (\eta + \kappa)k_B T \dot{N}_{ev}$ , where the atom loss rate due to evaporation is  $N_{ev}/N = -2(\eta - 4)e^{-\eta} \gamma_{el}/(2\sqrt{2})$  [12,23,36]. The second mechanism results from the decrease in the oscillation frequency due to the adiabatic reduction of the trap depth, leading to a rate  $\dot{E}_{ad} = E \dot{U}/(2U)$  for a harmonic trap. The third mechanism is heating due to spontaneous emission induced by the dipole

trap laser. We model the associated variation of energy as  $\dot{E}_{\text{heat}} = 2E_r R N$ , where  $E_r$  is the recoil energy gained in the scattering of a photon by an atom, which occurs at a rate  $R(t) \propto U(t)$ . Finally, the energy varies due to the loss of atoms by one-, two-, or three-body inelastic collisions. Each  $q$ -body loss ( $q = 1, 2$ , or  $3$ ) is governed by the equation for the local density  $\dot{n}_q(\mathbf{r}, t) = -K_q n(\mathbf{r}, t)^q$ . It gives the rate of variation in the energy

$$\dot{E}_q = \frac{3}{2} \dot{N}_q k_B T + \int U(\mathbf{r}) \dot{n}_q(\mathbf{r}, t) d^3 \mathbf{r}, \quad (1)$$

where the first and second terms are the contributions of the kinetic energy and of the trapping potential  $U(\mathbf{r})$ , respectively [12]. Here,  $\dot{N}_q = \int \dot{n}_q(\mathbf{r}, t) d^3 \mathbf{r}$ . Plugging in the equation for the evolution of the local density yields

$$\dot{E}_q = \left(\frac{3}{2} + \gamma_q\right) \dot{N}_q k_B T, \quad (2)$$

where

$$\gamma_q = \frac{1}{q} \frac{T}{V_q} \frac{dV_q}{dT} \quad \text{and} \quad V_q = \int e^{-q \frac{U(\mathbf{r})}{k_B T}} d^3 \mathbf{r}. \quad (3)$$

For an infinitely deep harmonic trap, we find  $\gamma_q = 3/(2q)$ , showing that two- and three-body losses carry away less than the average energy, leading to anti-evaporation. This is due to the fact that these losses occur mainly at the center of the trap, where the density is highest and the energy of the atoms is lower than the average energy. The atom loss rate due to  $q$ -body inelastic collisions is  $\dot{N}_q/N = -K_q n_0^{q-1}/(q\sqrt{q})$ .

Using  $\dot{N} = \dot{N}_{\text{ev}} + \sum_q \dot{N}_q$  and  $\dot{E} = \dot{E}_{\text{ev}} + \dot{E}_{\text{ad}} + \dot{E}_{\text{heat}} + \sum_q \dot{E}_q$ , we obtain the set of coupled equations governing the evaporation in the presence of heating and  $q$ -body losses:

$$\begin{aligned} \frac{\dot{N}}{N} &= -2(\eta - 4)e^{-\eta} \frac{\gamma_{\text{el}}}{2\sqrt{2}} + \sum_{q=1,2,3} \frac{\dot{N}_q}{N}, \\ \frac{\dot{T}}{T} &= -2 \left( \frac{\eta + \kappa}{3} - 1 \right) (\eta - 4) e^{-\eta} \frac{\gamma_{\text{el}}}{2\sqrt{2}} \\ &+ \sum_{q=1,2,3} \frac{1}{3} \left( \frac{3}{2} + \gamma_q - 3 \right) \frac{\dot{N}_q}{N} + \frac{2E_r}{3k_B T} R + \frac{\dot{U}}{2U}, \end{aligned} \quad (4)$$

where  $\eta$ ,  $R$ , and  $\gamma_{\text{el}}$  are functions of time. We solve these equations numerically using the experimental ramp  $U(t)$  in Fig. 2. We find that the heating rate  $R(t)$ , which amounts initially to  $R(0) = 22 \text{ s}^{-1}$ , drops very rapidly and has very little influence on evaporation. For the one-body loss rate, we plug into the simulation the value  $K_1 = 0.1 \text{ s}^{-1}$ , corresponding to the measured 10-s vacuum-limited lifetime of a single atom in the microscopic trap [25]. Also, for the three-body loss rate we take the value that we measured in a separate experiment,  $K_3 = 4 \times 10^{-29} \text{ cm}^6 \text{ s}^{-1}$  [37]. To reproduce our data more accurately we have to assume a two-body loss rate  $K_2 = 1.5 \times 10^{-14} \text{ cm}^3 \text{ s}^{-1}$ . The two-body losses may be due to a small steady population of atoms in state  $F = 2$  caused by the near-resonant laser being switched off improperly. This population results in hyperfine changing collisions with the atoms in the  $F = 1$  level. Reference [38] reports a value for the hyperfine changing collision rate of  $8 \times 10^{-12} \text{ cm}^3 \text{ s}^{-1}$ . We infer from this value a fraction of atoms in the  $F = 2$  states of 0.2%, too small to be measured directly with our setup.

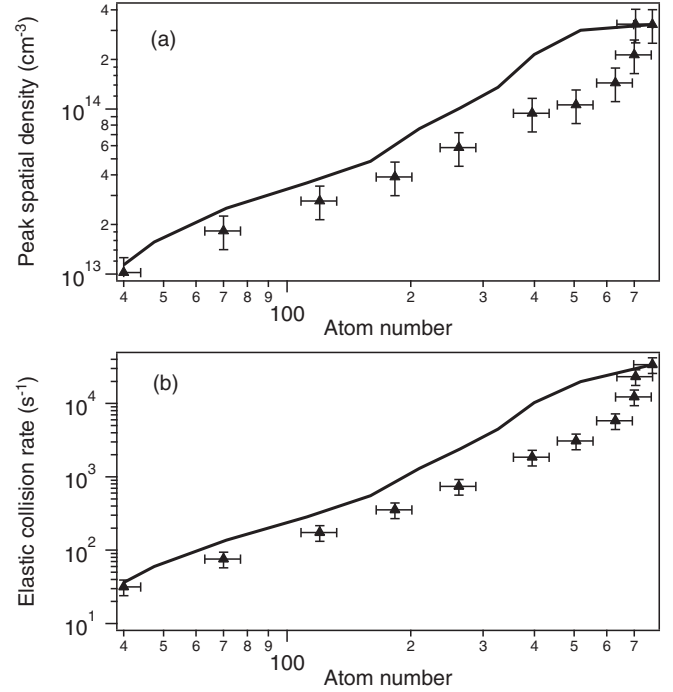


FIG. 4. Evolution of (a) the spatial density  $n_0$  and (b) the elastic collision rate  $\gamma_{\text{el}} = n_0 \sigma \bar{v} \sqrt{2}$  at the center of the trap, versus the number of atoms. Triangles: values extracted from the measurements of  $T$ ,  $N$ , and the trap depth  $U$ . Error bars correspond to 10% uncertainties on  $T$ ,  $N$ , and the oscillation frequency  $\omega$ . Solid lines: kinetic model using  $\sigma = \epsilon 4\pi a^2$  with  $\epsilon = 4/3$  (i.e., atoms are equally distributed among the Zeeman sublevels of  $F = 1$ ).

The contributions of the two- and three-body losses in Eqs. (4) are significant essentially at the beginning of the ramp, where the loss rates amount to  $K_2 n_0 / (2\sqrt{2}) \simeq 1.7 \text{ s}^{-1}$  and  $K_3 n_0^2 / (3\sqrt{3}) \simeq 0.8 \text{ s}^{-1}$ , respectively. As shown in Fig. 4(a), the density drops below  $10^{14} \text{ cm}^{-3}$  when the number of atoms becomes smaller than 400. Inelastic losses thus become negligible. This justifies the experimental validity of the scaling laws detailed in Sec. III. For  $N \leq 400$ , the main contributions to the evaporation process are the adiabatic reduction of the trap depth and the elastic collision rate, which has decreased by  $\sim 3$  orders of magnitude by the end of the ramp [see Fig. 4(b)].

Using the above-mentioned parameters for the heating and inelastic loss rates, Eqs. (4) yield the evolution of the temperature, number of atoms, and phase-space density as a function of the evaporation time. Figure 5 compares the experimental data with the results of the model for values of the elastic cross section  $4/3 \leq \sigma / (4\pi a^2) \leq 2$ . The agreement between the simulation and the data is better than 30% for the temperature and the parameter  $\eta$  [see Fig. 5(a) and inset]. By setting  $K_2 = 0$  and  $K_3 = 0$  in the simulation, we have checked that the inelastic losses at the beginning of the ramp are largely responsible for the decrease in  $\eta$  in the early stage of the evaporation. The agreement between the model and the data is somewhat less satisfactory for the number of atoms [see Fig. 5(b)]. In particular,  $N$  decreases experimentally more slowly than predicted at the beginning of the ramp. This could be due to the fact that the model does not account for the

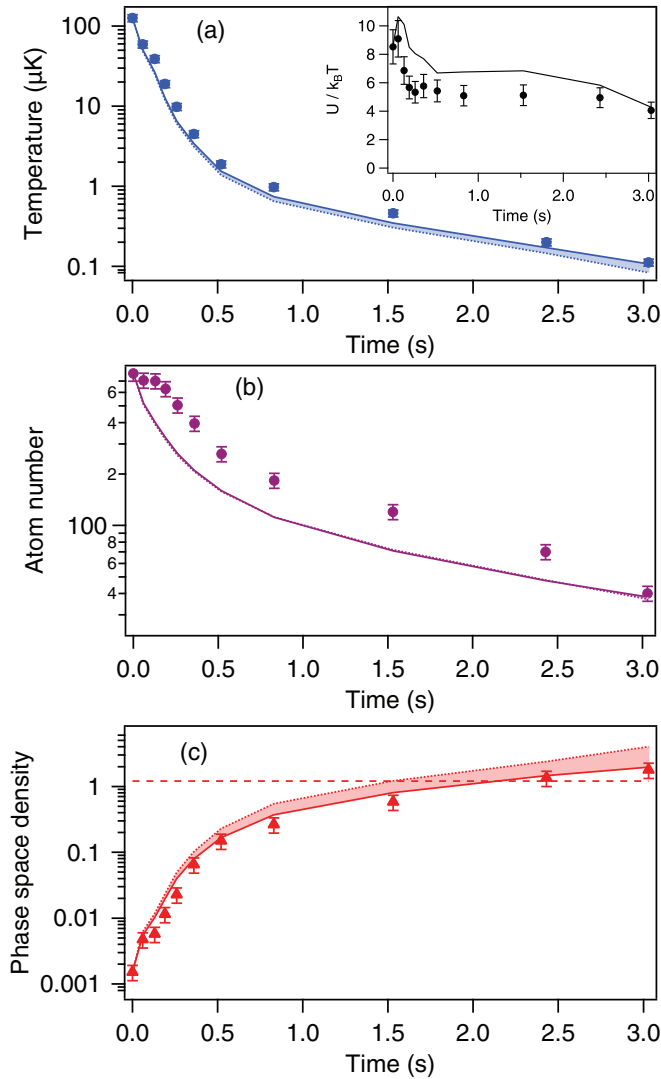


FIG. 5. (Color online) Comparison between the data and the model of Eqs. (4). Evolution of (a) the temperature  $T$ , (b) the number of atoms  $N$ , and (c) the phase-space density  $D = N(\hbar\omega/k_B T)^3$ , as a function of the evaporation time. The dots and triangles are the data. Error bars correspond to 10% uncertainties on  $T$ ,  $N$  and the oscillation frequency  $\omega$ . The solid and dotted lines are respectively the predictions of the model for  $\sigma = (4/3) \times 4\pi a^2$  (i.e. the atoms are equally distributed among the Zeeman sub-levels of  $F = 1$ ) and  $\sigma = 2 \times 4\pi a^2$  (i.e. the atoms are all in the same Zeeman sub-level). Here, we have taken  $\{K_1; K_2; K_3\} = \{0.1 \text{ s}^{-1}; 1.5 \times 10^{-14} \text{ cm}^3 \text{ s}^{-1}; 4 \times 10^{-29} \text{ cm}^6 \text{ s}^{-1}\}$ . In (c), the dashed line corresponds to  $D = \zeta(3) \simeq 1.202$ . Inset in (a) : evolution of  $\eta = U/k_B T$ .

possible hydrodynamic behavior at the beginning of the ramp, as mentioned in Sec. III. It could also derive from the fact that evaporated atoms remain in the vicinity of the trap when

we perform imaging of the cloud (and therefore contribute to the measured number of atoms) but do not collide with the remaining trapped atoms (and therefore do not contribute to evaporation at a later time). Finally, Fig. 5(c) shows a good agreement between the simulation and the data for the phase-space density. The slowing-down of evaporation seen in both the experiment and the theory is a consequence of the decrease in the elastic collision rate when the trapping potential is lowered, even in the absence of inelastic losses (see, e.g., [23]). In our case, inelastic losses further slow down the evaporation process at the beginning of the evaporation: in the absence of these losses (but with the same microscopic trapping potential and evaporation ramp), the phase-space density would reach unity after 700 ms only.

## V. CONCLUSION

In conclusion, we have implemented evaporative cooling of a few hundred atoms held in a microscopic dipole trap. After an evaporation period of 3 s we reach a phase-space density of  $\sim 2$  with 40 unpolarized atoms at  $\sim 100$  nK, close to quantum degeneracy. The overall duty cycle of the experiment is around 4 s. The atomic sample thus obtained is a good starting point for experiments involving mesoscopic-sized ultracold atomic samples. In the future, it will be interesting to enhance the efficiency of the evaporation by tilting the potential, e.g., by applying a strong magnetic field gradient [7,39] or an extra laser beam to achieve the runaway regime [40]. This may allow us to reach Bose-Einstein condensation with a small number of atoms and to decrease the duration of the evaporation.

From a theoretical perspective, we have compared our data to a simple model of evaporative cooling, assuming the trapping potential to be harmonic. We have found that the scaling laws governing the evolution of the thermodynamics quantities are still relevant in our regime of small atom numbers, as long as the ratio  $\eta$  remains constant and the inelastic losses are negligible. We have also found that a kinetic model taking into account time variations of  $\eta$  as well as heating and loss mechanisms reproduces the dynamics of the evaporation in a fair way. This simple model is therefore a useful guide to optimize evaporation parameters. In the future it will be interesting to refine the model presented here by taking into account the real shape of the Gaussian laser trap potential [41,42].

## ACKNOWLEDGMENTS

We thank T. Lahaye for careful reading of the manuscript. We acknowledge support from the E.U. through the ERC Starting Grant ARENA and the AQUITE Project and from the Region Ile de France (Triangle de la Physique and IFRAF).

- [1] M. Saffman and T. G. Walker, *Phys. Rev. A* **66**, 065403 (2002).  
 [2] M. D. Lukin, M. Fleischhauer, R. Coté, L. M. Duan, D. Jaksch, J. I. Cirac, and P. Zoller, *Phys. Rev. Lett.* **87**, 037901 (2001).

- [3] M. Saffman, T. G. Walker, and K. Mølmer, *Rev. Mod. Phys.* **82**, 2313 (2010).  
 [4] D. Maxwell, D. J. Szwer, D. Paredes-Barato, H. Busche, J. D. Pritchard, A. Gauguier, K. J. Weatherill, M. P. A. Jones, and C. S. Adams, *Phys. Rev. Lett.* **110**, 103001 (2013).

- [5] Y. O. Dudin and A. Kuzmich, *Science* **336**, 887 (2012).
- [6] T. Grünzweig, A. Hilliard, M. McGovern, and M. F. Andersen, *Nature Phys.* **6**, 951 (2010).
- [7] F. Serwane, G. Zürn, T. Lompe, T. B. Ottenstein, A. N. Wenz, and S. Jochim, *Science* **332**, 336 (2011).
- [8] D. M. Stamper-Kurn, H.-J. Miesner, A. P. Chikkatur, S. Inouye, J. Stenger, and W. Ketterle, *Phys. Rev. Lett.* **81**, 2194 (1998).
- [9] D. Jacob, E. Mimoun, L. De Sarlo, M. Weitz, J. Dalibard, and F. Gerbier, *New J. Phys.* **13**, 065022 (2011).
- [10] S. Whitlock, R. Gerritsma, T. Fernholz, and R. J. C. Spreeuw, *New J. Phys.* **11**, 023021 (2009).
- [11] J. Sebby-Strabley, R. T. R. Newell, J. O. Day, E. Brekke, and T. G. Walker, *Phys. Rev. A* **71**, 021401 (2005).
- [12] O. J. Luiten, M. W. Reynolds, and J. T. M. Walraven, *Phys. Rev. A* **53**, 381 (1996).
- [13] W. Ketterle and N. J. Van Druten, *Adv. At. Mol. Opt. Phys.* **37**, 181 (1996).
- [14] C. S. Adams, H. J. Lee, N. Davidson, M. Kasevich, and S. Chu, *Phys. Rev. Lett.* **74**, 3577 (1995).
- [15] M. D. Barrett, J. A. Sauer, and M. S. Chapman, *Phys. Rev. Lett.* **87**, 010404 (2001).
- [16] S. R. Granade, M. E. Gehm, K. M. O'Hara, and J. E. Thomas, *Phys. Rev. Lett.* **88**, 120405 (2002).
- [17] G. Cennini, G. Ritt, C. Geckeler, and M. Weitz, *Appl. Phys. B* **77**, 773 (2003).
- [18] T. Weber, J. Herbig, M. Mark, H.-C. Nägerl, and R. Grimm, *Science* **299**, 232 (2003).
- [19] T. Kinoshita, T. Wenger, and D. S. Weiss, *Phys. Rev. A* **71**, 011602 (2005).
- [20] R. Dumke, M. Johanning, E. Gomez, J. D. Weinstein, K. M. Jones, and P. D. Lett, *New J. Phys.* **8**, 64 (2006).
- [21] T. Gerricke, P. Würtz, D. Reitz, C. Utfeld, and H. Ott, *Appl. Phys. B* **89**, 447 (2007).
- [22] T. Lauber, J. Küber, O. Wille, and G. Birkl, *Phys. Rev. A* **84**, 043641 (2011).
- [23] K. M. O'Hara, M. E. Gehm, S. R. Granade, and J. E. Thomas, *Phys. Rev. A* **64**, 051403 (2001).
- [24] D. Comparat, A. Fioretti, G. Stern, E. Dimova, B. Laburthe Tolra, and P. Pillet, *Phys. Rev. A* **73**, 043410 (2006).
- [25] Y. R. P. Sortais, H. Marion, C. Tuchendler, A. M. Lance, M. Lamare, P. Fournet, C. Armellin, R. Mercier, G. Messin, A. Browaeys, and P. Grangier, *Phys. Rev. A* **75**, 013406 (2007).
- [26] A. Fuhrmanek, R. Bourgain, Y. R. P. Sortais, and A. Browaeys, *Phys. Rev. A* **85**, 062708 (2012).
- [27] A. Fuhrmanek, Y. R. P. Sortais, P. Grangier, and A. Browaeys, *Phys. Rev. A* **82**, 023623 (2010).
- [28] It could happen that a minor gain in phase space resulted in an important loss of atoms. In this case we kept the ramp corresponding to the largest number of atoms.
- [29] H. C. W. Beijerinck, *Phys. Rev. A* **62**, 063614 (2000).
- [30] W. Ketterle and N. J. van Druten, *Phys. Rev. A* **54**, 656 (1996).
- [31] G. Grynberg, B. Lounis, P. Verkerk, J.-Y. Courtois, and C. Salomon, *Phys. Rev. Lett.* **70**, 2249 (1993).
- [32] A. M. Kaufman, B. J. Lester, and C. A. Regal, *Phys. Rev. X* **2**, 041014 (2012).
- [33] J. D. Thompson, T. G. Tiecke, A. S. Zibrov, V. Vuletić, and M. D. Lukin, *Phys. Rev. Lett.* **110**, 133001 (2013).
- [34] These two determinations of  $\eta$  are independent, as the calculation of the phase-space density depends also on the value of the trap depth.
- [35] This expression of  $\kappa$  holds only in the limit  $\eta \gg 1$ . To account for our not-so-large values of  $\eta$  at the end of the evaporation ramp, we could use the general expression of  $\kappa = 1 - P(5, \eta)/(\eta P(3, \eta) - 4P(4, \eta))$ , where  $P$  is the incomplete  $\gamma$  function [45]. We checked that this alters the overall results in  $N$  and  $T$  by less than a few percent.
- [36] This expression of  $\dot{N}_{\text{ev}}/N$  holds for  $\eta \gg 1$ . We also checked that using the general expression  $\dot{N}_{\text{ev}}/N = -2(\eta P(3, \eta) - 4P(4, \eta))e^{-\eta} \gamma_{\text{el}}/(2\sqrt{2})$  does not significantly change the result of the simulation.
- [37] Our value  $K_3 = 4 \pm 3 \times 10^{-29} \text{ cm}^6/\text{s}$ , measured on a cloud at a temperature of 100  $\mu\text{K}$ , is compatible with the values obtained in [43] and [44] at much lower temperatures.
- [38] S. D. Gensemer, P. L. Gould, P. J. Leo, E. Tiesinga, and C. J. Williams, *Phys. Rev. A* **62**, 030702 (2000).
- [39] C.-L. Hung, X. Zhang, N. Gemelke, and C. Chin, *Phys. Rev. A* **78**, 011604 (2008).
- [40] J.-F. Clément, J.-P. Brantut, M. Robert-de-Saint-Vincent, R. A. Nyman, A. Aspect, T. Bourdel, and P. Bouyer, *Phys. Rev. A* **79**, 061406 (2009).
- [41] L. Simon and W. T. Strunz, *Phys. Rev. A* **81**, 063620 (2010).
- [42] Y. R. P. Sortais *et al.*, in preparation (2013).
- [43] E. A. Burt, R. W. Ghrist, C. J. Myatt, M. J. Holland, E. A. Cornell, and C. E. Wieman, *Phys. Rev. Lett.* **79**, 337 (1997).
- [44] J. Söding, D. Guéry-Odelin, P. Desbiolles, F. Chevy, H. Inamori, and J. Dalibard, *Appl. Phys. B* **69**, 257 (1999).
- [45] M. Abramowitz and I. A. Stegun, eds., *Handbook of Mathematical Functions* (Dover, New York, 1972).