Coherent excitation of a nonlinear microcavity
Jérémy Oden, Stephane Trebaol, Philippe Delaye, Nicolas Dubreuil

To cite this version:

HAL Id: hal-00847306
https://hal-iogs.archives-ouvertes.fr/hal-00847306
Submitted on 23 Jul 2013

HAL is a multi-disciplinary open access archive for the deposit and dissemination of scientific research documents, whether they are published or not. The documents may come from teaching and research institutions in France or abroad, or from public or private research centers.

L’archive ouverte pluridisciplinaire HAL, est destinée au dépôt et à la diffusion de documents scientifiques de niveau recherche, publiés ou non, émanant des établissements d’enseignement et de recherche français ou étrangers, des laboratoires publics ou privés.
Coherent excitation of a nonlinear microcavity

J. Oden
Laboratoire Charles Fabry, Institut d’Optique, CNRS, Univ Paris Sud, 2 Avenue Augustin Fresnel, 91127 PALAISEAU cedex, FRANCE

S. Trebaol
Laboratoire Charles Fabry, Institut d’Optique, CNRS, Univ Paris Sud, 2 Avenue Augustin Fresnel, 91127 PALAISEAU cedex, FRANCE

P. Delaye
Laboratoire Charles Fabry, Institut d’Optique, CNRS, Univ Paris Sud, 2 Avenue Augustin Fresnel, 91127 PALAISEAU cedex, FRANCE

N. Dubreuil
nicolas.dubreuil@institutoptique.fr
Laboratoire Charles Fabry, Institut d’Optique, CNRS, Univ Paris Sud, 2 Avenue Augustin Fresnel, 91127 PALAISEAU cedex, FRANCE

Coherent excitation of a nonlinear semiconductor microcavity is theoretically reported. It intends to counterbalance the frequency drift of the cavity resonance driven by the nonlinear refractive effects, which causes a limitation in the energy coupling efficiency of an input pulse into the cavity resonance. We show that exciting such a nonlinear microcavity with tailored chirped pulses allows to maintain the benefit of light localization and to further enhance light-matter interactions, opening the way to the realization of highly efficient nonlinear devices.

[DOI: http://dx.doi.org/10.2971/jeos.2013.13046]

Keywords: Optical microcavities, nonlinear optics, coherent control, photonic crystal microcavities

1 INTRODUCTION

Photonic crystal microcavities with high-quality factor and very small mode volume allow a strong enhancement of light-matter and nonlinear interactions [1]. Among the various key components for photonic signal processing, realizations of all-optical switches based on nonlinear photonic crystal microcavities have been reported in Silicon [2], InP [3] (containing quantum wells), GaAs [4], InGaAs [5], and GalnP [6]. In such a device, a control pulse induces a refractive index change of the nonlinear material, which in turns shifts the resonance frequency and modifies the transmission of the cavity. The refractive index variation is achieved through the plasma effect of carriers generated by either one-photon [3] or two-photon absorption [2, 4, 5], and ultimately by means of the optical Kerr effect [6]. Whereas the nonlinear refractive index change induced by the pulse front edge detunes the cavity resonance, it also contributes to a decrease of the coupling efficiency for the rest of the pulse. It means that only one part of the pulse energy is effective to perform the optical switching operation. Despite this limitation in the energy coupling efficiency, the mismatch between the time varying resonance frequency and the excitation pulse frequency leads to a ringing behavior [7, 8], and induces temporal distortions of the pulse [9].

In order to maintain the benefit of light localization throughout the pulse excitation and to control the intracavity field dynamics, we study in this article the behavior of a nonlinear microcavity excited by a tailored chirped pulse. The spectral components of the excited pulse are set to compensate for the nonlinear frequency drift of the cavity resonance. This approach is based on the pulse shaping techniques that are commonly used for the coherent excitation of atomic and molecular systems [10]–[12], and which start now to be theoretically investigated in nonlinear microcavities [13, 14]. Sandhu et. al. [13] have studied a phase-shaped pulse excitation that compensates for the intrinsic linear dispersion of the cavity resonance, in order to reduce the switching threshold power of a bistable Kerr microcavity. Very recently, Kristensen et. al. [14] have demonstrated fast switching of a pure-Kerr microcavity in a controlled two-pulse excitation scheme.

While references [13] and [14] deal with cavities operating under pure Kerr effect, we consider a more realistic nonlinear semiconductor microcavity driven by the optical Kerr effect, the two-photon absorption (TPA), the free carrier refraction (FCR) and absorption (FCA) effects induced by the free carriers generated by TPA. In a first section, we present the model used to simulate the dynamic behavior of the intracavity field. It is based on the coupled mode theory [15, 16] and includes the nonlinear effects listed above. We next study the dynamics of a silicon based microcavity under a linearly chirped pulse excitation. By compensating for the nonlinear frequency drift of the cavity resonance, using an appropriate phase relation between the spectral components of the input pulse, we show an improvement in the intracavity time-averaged stored energy and an enhancement of the nonlinear interactions. We conclude by discussing the interest of such a coherent excitation as a means to control the dynamics of nonlinear microcavities.
2 MODEL

We consider the nonlinear dynamics of an electromagnetic field circulating inside a cavity coupled to a bus waveguide in a side-coupled geometry depicted in Figure 1. The field amplitude is defined as \( u(t) = \sqrt{P(t)} \exp(i \phi(t)) \), where \( P(t) \) is the intra-cavity optical power, \( \phi(t) = \arg[u(t)] \) the intra-cavity field phase, \( T_R \) the cavity round-trip time. Using the coupled mode theory, its temporal evolution is given by \([15, 16]\)

\[
\frac{du}{dt} = -\frac{1}{\tau} + \frac{1}{\tau_{\text{NL}}(t)} u(t) + i \omega_{\text{res}0} \left( 1 + \frac{\Delta \omega_{\text{res}}(t)}{\omega_{\text{res}0}} \right) u(t) + \frac{\sigma_a}{\tau_c} s_{\text{in}}(t), \tag{1}
\]

where \( |s_{\text{in}}(t)|^2 \) is the instantaneous power of the input signal and \( \omega_{\text{res}0} \) is the resonance frequency of the cavity set in the linear regime. The linear cavity photon lifetime \( \tau/2 \) corresponds to \( 1/\tau = 1/\tau_0 + 1/\tau_c \), where \( \tau_0/2 \) and \( \tau_c/2 \) are the photon lifetimes respectively related to the intrinsic cavity linear losses and to the coupling constant between the waveguide and the cavity. The nonlinear effects are included in the first two terms of the right-hand side of Eq. (1). The parameter \( \tau_{\text{NL}} \), which depends on the intracavity mode amplitude \( u \), depicts the modification of the cavity photon lifetime through the nonlinear absorption effects. The time dependent frequency shift of the cavity resonance induced by the nonlinear refractive index change of the medium is described by the term \( \Delta \omega_{\text{res}}(t) \). Notice that Eq. (1) assumes a slowly-varying field amplitude \( u(t) \) within the cavity round-trip time \( \tau_R \).

In the next section, we will consider the nonlinear behavior of a silicon based microcavity operating around 1550 nm. Although one photon energy (0.8 eV) is smaller than the silicon band gap energy (\( \sim 1.1 \) eV), nonlinear absorption occurs due to two photon absorption, which is accompanied by the simultaneous generation of free carriers. The two related nonlinear absorption effects, respectively TPA and FCA, are included in the parameter \( \tau_{\text{NL}}(t) \) through the relation \( 1/\tau_{\text{NL}}(t) = 1/\tau_{\text{TPA}}(t) + 1/\tau_{\text{FCA}}(t) \)[16], with

\[
\frac{1}{\tau_{\text{TPA}}} = \frac{\beta_{\text{TPA}} c_0^2}{2n_0^2 V} |u(t)|^2, \quad \frac{1}{\tau_{\text{FCA}}} = \frac{\sigma_a c_0}{2n_0} N(t). \tag{2}
\]

The TPA photon lifetime \( \tau_{\text{TPA}}/2 \) depends on the two-photon absorption coefficient \( \beta_{\text{TPA}} \), the effective linear refractive index of the cavity material \( n_0 \), the speed of light \( c_0 \), and the Kerr volume \( V \). The FCA photon lifetime \( \tau_{\text{FCA}}/2 \) is expressed in terms of the FCA cross section \( \sigma_a \) and the free carrier density \( N(t) \) with a temporal evolution governed by:

\[
\frac{dN(t)}{dt} + \frac{1}{\tau_c} N(t) = \frac{\beta_{\text{TPA}}}{2n_0^2} \left( \frac{|c_0 u(t)|^2}{n_0^2 V} \right)^2, \tag{3}
\]

where \( \tau_c \) is the carrier lifetime. For the sake of simplicity, we have approximated the free-carrier effects volume to the Kerr volume. We have also neglected the linear dispersion of the cavity material such as the group index is approximated to \( n_0 \). The nonlinear refractive index variation \( \Delta n(t)/n_0 \), governed by both the Kerr effect and the FCR, modifies the resonance frequency through the relation:

\[
\frac{\Delta \omega_{\text{res}}(t)}{\omega_{\text{res}0}} = - \frac{\Delta n(t)}{n_0} = - \frac{n_2 c}{n_0^2 V} |u(t)|^2 - \sigma_r n_0 |u(t)|^2. \tag{4}
\]

The first term on the right-hand side corresponds to the optical Kerr effect, where \( n_2 \) is the Kerr coefficient, and the second one is related to the FCR effect, with \( \sigma_r \) the effective volume of free carrier refraction. According to the analysis conducted in [17], and considering our pulse excitation condition (few ps pulse duration and low repetition time around 10 ns), we have neglected the thermal refractive index variation related to the fast dynamics of the free carriers. Indeed, it has been evaluated two orders of magnitude lower than the free carrier refractive index change. Using Eqs. (1)–(4), we next study the temporal evolution of the intra-cavity field intensity.

3 NONLINEAR MICROCAVITY DYNAMICS

We consider a silicon based microcavity with a length \( L = 900 \) nm and an effective mode area \( A_{\text{eff}} = 300 \times 300 \) nm\(^2\), which leads to a cavity mode volume \( V = 0.081 \) \( \mu \)m\(^3\). The intrinsic and extrinsic losses are set to \( \tau_0 = 49.4 \) ps and \( \tau_c = 15 \) ps, leading to a quality factor \( Q = c/\tau = 7000 \) (with \( \tau = 11.5 \) ps). The nonlinear parameters for silicon around 1550 nm [16] are: \( n_2 = 4.4 \times 10^{-18} \) m\(^2\)/W, \( \beta_{\text{TPA}} = 8.4 \times 10^{-12} \) m/W, \( \sigma_r = -1.34 \times 10^{-27} \) m\(^2\)/s, and \( \sigma_a = 14.5 \times 10^{-22} \) m\(^2\). As the effective linear refractive index depends on the cavity structure, which is not defined here, it is set to the linear refractive index of silicon \( n_0 = 3.48 \), leading to \( \tau_0 = n_0 L/c = 10 \) fs. Moreover, the carrier lifetime \( \tau_c \) is assumed to be 0.4 ns (as measured in ref [16]), which is much longer than both the pulse duration and the cavity photon lifetime. We assume here that \( \tau_c \) is not affected by the nonlinear effects.

In this section, we study an excitation under a Fourier-transform-limited gaussian pulse with a full width at 1/\( e \) in intensity of 3.4 \( c \) and an incident peak power of 23 mW, corresponding to an energy of 780 fJ. The pulse duration is arbitrary chosen such that it is longer than \( \tau \) in order to avoid a transient excitation of the cavity [18]. When the pulse carrier frequency coincides with the resonance frequency \( \omega_{\text{res}0} \), the temporal evolution of the intra-cavity power \( P(t) \) is represented by the black solid line in Figure 2(a). The comparison with the incident pulse profile, given by the dashed line, shows a sudden drop of the intra-cavity power at the time \( t = -0.5 \tau \) followed by a damped oscillation. It actually coincides with the strong detuning of the cavity resonance \( \Delta \omega_{\text{res}}(t) \) reported in Figure 2(b) with the black...
pulse phase $φ$ could be counter-balanced by a proper tailoring of the input mismatch tends to reduce the intra-cavity field energy, which both the linear and nonlinear losses. Consequently, this phase mismatch between the time varying phase of the intra-cavity field and the fixed phase of the input pulse gives rise to a situation where the beat between the intra-cavity field and the input pulse is manifested by a source term (right-hand side), namely the beat term $(\text{right-hand side})$. This equation describes the damping (left-hand side) of a source term (right-hand side), namely the beating between the intra-cavity field and the input pulse. The mismatch between the time varying phase $φ_u(t)$ of the intra-cavity field and the fixed phase of the input pulse gives rise to the oscillating behavior with a damping rate governed by both the linear and nonlinear losses. Consequently, this phase mismatch tends to reduce the intra-cavity field energy, which could be counter-balanced by a proper tailoring of the input pulse phase $φ_{in}(t)$ as it will be shown in Section 4.

In order to show that the reduction of the stored energy is mainly governed by the nonlinear refractive effects, we next perform a simulation for which the nonlinear frequency shift is omitted, i.e. by setting $δω_{res}(t) = 0$ in Eq. 1. Note that such a situation would be equivalent to consider an input pulse with a tailored phase-shape $φ_{in}(t) = φ_u(t)$, perfectly compensating the nonlinear refraction induced frequency drift of the cavity resonance. The corresponding temporal evolution of the intra-cavity field is represented by the solid blue line in Figure 2(a). Despite nonlinear absorption effects, the stored energy is higher than in the former simulation that includes the refractive effects (curves in black solid line). To quantify this improvement, we introduce a magnification factor defined as the ratio between the time averaged intra-cavity field power and the time-averaged input pulse power:

$$
M_{\text{eff}} = \frac{\int_{-\infty}^{+\infty} P_{in}(t)dt}{\int_{-\infty}^{+\infty} |s_{in}(t)|^2dt}. \tag{6}
$$

According to this definition, the calculated magnification factor for the black curve in Figure 2(a) is $M_{\text{eff}} = 130$, while it reaches $M_{\text{eff}} = 265$ for the blue curve. Moreover, the generated carrier density calculated for the latter is 3 times higher than in the former, which shows an enhancement of the light-matter interaction within the cavity in the case of a tailored phase-shaped pulse.

In the next section, we will demonstrate that, using an appropriate linearly chirped pulse, the beating effect between the incident and the intra-cavity fields is reduced and its interaction with the intra-cavity nonlinear material can be enhanced.

4 COHERENT EXCITATION OF A NONLINEAR MICROCAVITY

In the case of a gaussian pulse and assuming a carrier lifetime longer than the pulse duration, the resonance drift depicted in Figure 2(b) can be approximated by an error function (see Eq. (3) and [19]). Therefore, we can study the cavity behavior under a linearly chirped pulse excitation with a spectral phase relation that fairly approximates the resonance drift. A linearly chirped pulse is achieved through the propagation of a transform limited pulse $s_{\text{initial}}$ inside a second order dispersive medium (see left-inset in Figure 1).

Hereafter, the initial transform-limited pulse $s_{\text{initial}}$ follows a gaussian shape:

$$
s_{\text{initial}}(t) = \sqrt{P_0} \exp \left[-\frac{t^2}{2T_p^2}\right] e^{i(ω_{\text{res}} + δω)t}, \tag{7}
$$

where $δω = ω_0 - ω_{\text{res}}$ is the frequency detuning between the pulse and the cavity resonance. At the output of the dispersive medium, the chirped pulse is expressed

$$
s_{\text{chirped}}(t) = \sqrt{\frac{P_0}{T_p}} P_0 \exp \left[-\frac{t^2}{2T_p^2} + i \frac{1}{2} α t^2\right] e^{i(ω_{\text{res}} + δω)t}, \tag{8}
$$

where $T_p$ and $α$ are related to the second order dispersion co-
The remaining parameter is the initial detuning frequency $\delta \omega$. Intuitively, the chirped-pulse should be blue-shifted respectively to the initial cavity resonance by one-half of the non-linear frequency blue-shift. A more accurate analysis is conducted by computing the intra-cavity field dynamics, setting $s_{\text{in}}(t) = s_{\text{chirped}}(t)$ in Eqs. (1) with the previously defined parameters, for $\delta \omega$ detunings varying between 0 and 20/τ. Following the previous section, we have plotted in Figure 3 the effective magnification factor $M_{\text{eff}}$ calculated for the different detuning values (see the red curve). The time-averaged stored energy increases along with a blue detuning. The maximum value $M_{\text{eff}} = 225$ is obtained for $\delta \omega = 9/\tau$, which is nearby the value we have anticipated. For a larger detuning, the initial coupling efficiency of the pulse with the cavity resonance is too weak to efficiently generate free carriers and to initiate a blue shift of the cavity.

As the Fourier-transform-limited gaussian pulse exhibits a ringing behavior on the intra-cavity field dynamics, the intra-cavity field shape under the chirped pulse excitation undergoes less distortions and leads to a higher magnification factor. This improvement is due to an accurately tailored chirped pulse, whose instantaneous frequency coincides with the non-linear resonance drift, which allows the light to efficiently build-up inside the cavity.

Lastly, we consider the case of the Fourier-transform-limited gaussian pulse with a non-zero detuning in order to emphasize the importance of the pulse phase-shaping. Similarly to the chirped pulse excitation, the intra-cavity field dynamics is computed for various values of $\delta \omega$. The calculated effective magnification factors are reported with the grey curve in Figure 3. The maximum value $M_{\text{eff}} = 170$ is reached for $\delta \omega \approx 4/\tau$. The corresponding intra-cavity dynamics plotted

For a strongly chirped pulse, we get $T_p \approx |\phi^{(2)}|/T_0$ and $\alpha \approx 1/|\phi^{(2)}|$.

We first need to set the parameters $T_0$, $P_0$, $\delta \omega$ of the initial pulse and the dispersion coefficient $\phi^{(2)}$. For the sake of comparison, the envelope characteristic of the chirped pulse is kept equal to that of the Fourier-transform limited gaussian pulse used in the previous section. Thus, we set its peak power to 23 mW, the pulse duration to $T_p = 1.7 \tau$, which gives a pulse energy of 780 fJ. The spectral linewidth of the pulse should now be consistent with the frequency shift experienced by the cavity resonance. As we have anticipated that 3 times more carrier density is expected with a tailored phase-shaped pulse, i.e. $\phi_{\text{in}}(t) = \phi_{\text{opt}}(t)$, the cavity blue-shift should reach $18/\tau$ (3 times the 6/τ blue-shift reported in Figure 2(b)). Following this expectation, the spectral linewidth of $s_{\text{initial}}(t)$ is set to $20/\tau$, corresponding to a pulse duration $T_0 = \tau/10$. The dispersion coefficient calculated from Eq. 9 is then set to $\phi^{(2)} = 0.17 \tau^2 = 22 \text{ps}^2$. By neglecting the propagation loss through the dispersive medium, the peak power of the initial pulse should be equal to $P_0 = 381$ mW (see Eq. 8).

The temporal evolution of the intra-cavity power achieved with the previously optimized chirped-pulse excitation is plotted with red solid line in Figure 4(a). Its temporal evolution is compared to the envelop intensity of the excited pulse (black dashed line) and to the intra-cavity power (black solid line) calculated in the previous section, with $\delta \omega = 0$. The dynamics of the resonance frequency drift achieved in both cases are reported in Figure 4(b). In the case of the tailored chirped pulse excitation, the resonance frequency drift reaches $16/\tau$, which is close to the expected value of $18/\tau$ in the case of the perfect phase control. The green line in Figure 4(b) shows the linear chirp of the input pulse, whose slope is $\alpha = 1/|\phi^{(2)}|$, which tangentially fits the resonance frequency drift during the whole excitation.

FIG. 3 Magnification factor variation with the frequency detuning $\delta \omega$ for both the chirped pulse (red line) and the transform-limited pulse (grey line).

FIG. 4 (a) Intra-cavity power and (b) cavity resonance frequency drift in the case of an initially on resonance transform-limited pulse (black lines), a transform-limited pulse with a numerically optimized frequency detuning (grey lines) and a linearly chirped pulse (red line) whose chirp is plotted in green (b). The input pulse profile is plotted with dashed line.
in Figure 4(a) (grey line) does not exhibit the ringing behavior that can be seen for the $\delta \omega = 0$ non-chirped gaussian pulse. Although this initial detuning slightly improves $M_{e_{ff}}$, it does not significantly increase the carrier density as the frequency blue-shift of the cavity resonance remains about $7/\tau$ (grey curve in Figure 4(b)).

5 CONCLUSION

The nonlinear dynamics of an optical microcavity subject to a nonlinear refractive induced frequency shift has been discussed in this article. Although an optical microcavity is used to enhance the light matter interaction, we have emphasized that the benefit of the light localization effect cannot be maintained throughout the pulse excitation because of the nonlinear refractive index change.

As an illustration, we have theoretically studied the intra-cavity intensity dynamics for a silicon based microcavity under a coherent pulse excitation. We have shown that a tailored linearly chirped pulse, for which the instantaneous frequency coincides with the nonlinear resonance drift, ensures a build-up of the intra-cavity energy. By doing so the light localization effect during the pulse excitation can be maintained, which leads to an enhancement of the intra-cavity nonlinear interaction. In our example, we have compared the excitation between a Fourier-transform-limited gaussian pulse and a tailored chirped pulse excitation. While the two pulses share the same gaussian shape with equal energy (780 fJ) and pulse duration (6.8 times the cavity photon lifetime), an enhancement by a factor of 3 of the free carrier density generated by two-photon absorption is reported in the latter case. Moreover, the intra-cavity field amplitude dynamics undergoes less deformation, illustrating the control of nonlinear dynamics by means of the pulse phase-shaping.

Besides the control of the nonlinear dynamics, such a coherent excitation enables to manipulate the effective optical bandwidth of micro cavities. Indeed, we have performed an efficient transfer of energy between an intra-cavity medium and a pulse whose spectral linewidth is 10 times larger than that of the linear cavity. Experiments are presently under progress to verify our theoretical predictions and to study the dependence between the chirp value and the energy of the input pulse.

The coherent excitation could be an efficient meaning to improve and to dynamically control the operation of microcavity-based all-optical devices. It could address the issue of their energy consumption and the control of more complex structures, such as coupled microcavities.

6 Acknowledgements

The authors acknowledge Robert Frey and Gilles Pauliat for highly valuable comments and discussions.

References